

Problem: Prove the striking identity

$$\sum_{k=0}^n \frac{(-1)^k}{2k+1} \binom{n}{k} = \frac{2 \cdot 4 \cdots (2n)}{3 \cdot 5 \cdots (2n+1)}$$